

Prophet: Fast Accurate Model-based Throughput Prediction for Reactive Flows in Data Center Networks

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Introduction

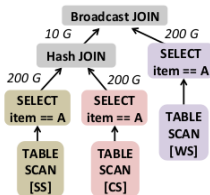
Throughput Prediction: Use Cases

Throughput prediction enables **network awareness** in applications.

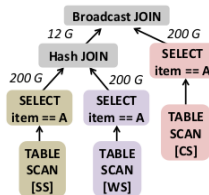
Query Plan Selection:

```
SELECT
  SS.item as item,
  SUM(SS.sales),
  SUM(WS.sales),
  SUM(CS.sales)
FROM store_sales SS,
     web_sales WS,
     cat_sales CS
WHERE SS.item == CS.item
      AND SS.item == WS.item
GROUP BY item
HAVING item STARTSWITH 'A'
```

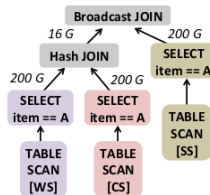
(a) A sample SQL Query



(b) QEP-1



(c) QEP-2



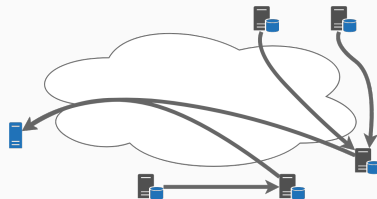
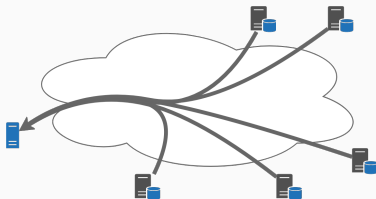
(d) QEP-3

Raajay Viswanathan et al. , CLARINET, OSDI'2016

Throughput Prediction: Use Cases

Throughput prediction enables **network awareness** in applications.

Transfers in Overlay Networks:



Reactive flows (most importantly, TCP) are widely used.

Data center network: *can be more than 99%*

In this paper, we make two major contributions. First, we measure and analyze production traffic (>150TB of compressed data), collected over the course of a month from ~6000 servers (§2), ex-

The measurements reveal that 99.91% of traffic in our data center is TCP traffic. The traffic consists of query traffic (2KB to 20KB in size), delay sensitive short messages (100KB to 1MB), and throughput sensitive long flows (1MB to 100MB). The query

Alizadeh *et al.* , DCTCP, SIGCOMM'2010

Reactive Flows

Reactive flows (most importantly, TCP) are widely used.

Internet: 80% - 90%

Table 1. Values of UDP/TCP Ratio.

Trace	Sample	UDP/TCP Ratio			Total IP Traffic (pkts/bytes/flows)
		pkts	bytes	flows	
CAIDA-OC48	08-2002	0.11	0.03	0.11	(1371M/838GB/79M)
	01-2003	0.12	0.05	0.27	(463M/267GB/26M)
GigaSUNET	04-2006	0.06	0.02	1.06	(422M/294GB/9M)
	11-2006	0.08	0.03	1.45	
CAIDA-OC192	06-2008	0.14	0.05	1.43	(4427M/2279GB/197M)
	02-2009	0.19	0.07	2.34	(1922M/1410GB/110M)
OptoSUNET	01-2009	0.21	0.11	3.09	(1100M/657GB/41M)
	02-2009	0.20	0.11	2.63	

CAIDA, Internet traffic analysis, 2002-2009

Throughput Prediction for Reactive Flows is Not Easy

Reactive flows interfere with each other.

Orange: Background flows Blue: New flows (to be predicted)



$$x_1 = x_2 = 200\text{Mbps}$$

$$x_3 = 200\text{Mbps}$$



$$x_1 = x_2 = 150\text{Mbps}$$

$$x_3 = x_4 = 150\text{Mbps}$$

Throughput Prediction for Reactive Flows is Not Easy

There exist different congestion control algorithms.

Solid: TCP Vegas Dashed: TCP Reno



$$x_1 = x_2 = 150\text{Mbps}$$

$$x_3 = x_4 = 150\text{Mbps}$$



$$x_1 = x_2 = ?\text{Mbps}$$

$$x_3 = ?\text{Mbps}, x_4 = ?\text{Mbps}$$

Throughput Prediction for Reactive Flows is Not Easy

Throughput can also be affected by source constraints.

Top: $x_4 \leq 180\text{Mbps}$ Bottom: $x_4 \leq 60\text{Mbps}$



$$x_1 = x_2 = 150\text{Mbps}$$

$$x_3 = x_4 = 150\text{Mbps}$$



$$x_1 = x_2 = 180\text{Mbps}$$

$$x_3 = 180\text{Mbps}, x_4 = 60\text{Mbps}$$

Summary

- Throughput prediction is useful
- Reactive flows (TCP) are widely used
- Throughput prediction for reactive flows is not easy
 - Reactive flows interfere with each other
 - Heterogeneous reactive mechanisms
 - The effects of source constraints

Basic Ideas

Motivation: Model-based Throughput Prediction

We want to answer this question (Q1):

Given a set of (TCP) flows, what is the expected throughput of each flow?

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Instead of answering it directly, we answer this question (Q2):

How does the network allocate bandwidth for TCP flows?

Motivation: Model-based Throughput Prediction

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Given a set of (TCP) flows, what is the expected throughput of each flow?

Instead of answering it directly, we answer this question (Q2):

How does the network allocate bandwidth for TCP flows?

There is an answer to this question!

Network Utility Maximization

$$\arg \max \sum U_i(x_i) \\ A\mathbf{x} \leq \mathbf{c}$$

(The allocation maximizes the total utility...)
(...subject to link capacity constraints)

Breakdown

To solve NUM (Q2), we need to answer the following questions:

Q3 *How do we know the utility function of each flow?*

Srikant's utility function $U_i(x_i) = \rho_i \frac{x_i^{1-\alpha_i}}{\alpha_i - 1}$ (leading to **Q6** and **Q7**).

Q4 *How do we obtain the capacity constraint information?*

Global location mapping, assuming non-blocking switch.

Q5 *How do we handle source constraints?*

Explicit declaration in queries and lazy identification in samples.

Further Breakdown

To compute Srikant's utility function (Q3), we need

Q6 *How do we obtain α_i ?*

Existing works by Oshio et al. .

Q7 *How do we obtain ρ_i ?*

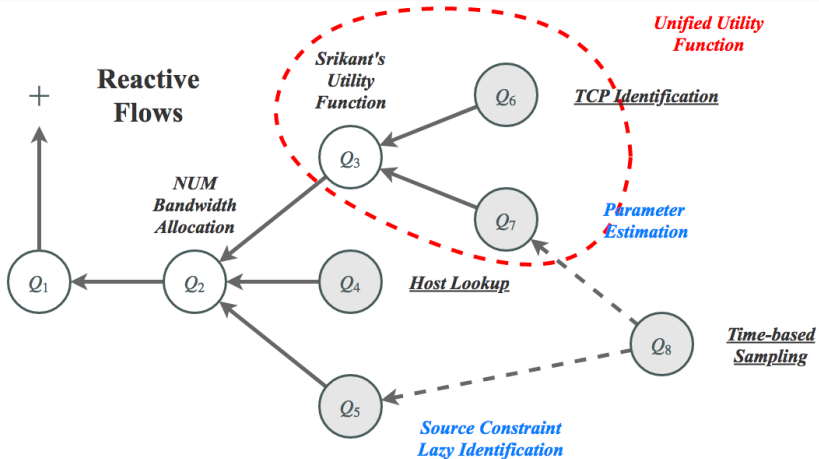
Parameter estimation by analyzing the **samples**.

Q8 *How do we get the samples?*

Time-based traffic mirroring.

Overview

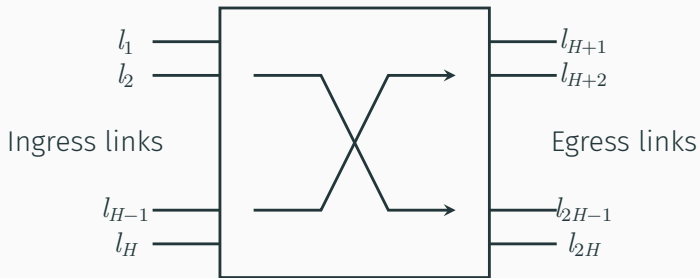
Throughput
Prediction



Problem Formulation

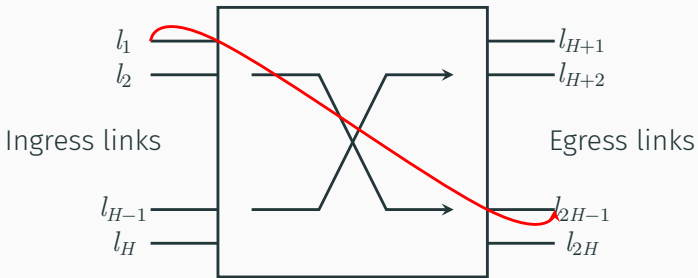
Network Model

We assume there are no bottlenecks in the core of the network (non-blocking switch assumption of DCN). The network is a bipartite graph. For a network with H hosts, there are $L = 2H$ links numbered as l_1, \dots, l_L and $\mathcal{L} = \{l_1, \dots, l_L\}$.



Flow Model

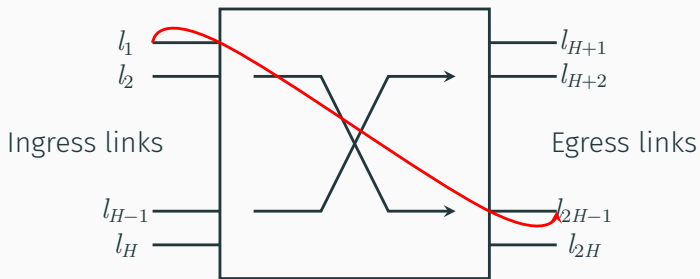
Assume there are N background flows numbered as f_1, \dots, f_N and M queried flows numbered as q_1, \dots, q_M . Let $\mathcal{F} = \{f_1, \dots, f_N\}$ and $\mathcal{Q} = \{q_1, \dots, q_M\}$. Let $A = \{a_{ij}\}_{L \times N}$ and $B = \{b_{ij}\}_{L \times M}$ be the **routing matrix**.



Flow Model (Cont.)

Let x_i be the throughput of f_i and y_i be the throughput of q_i . Let τ_i be the source constraint of f_i and π_i be the source constraint of q_i . Let

$$\mathbf{x} = \{x_1, \dots, x_N\}^T, \mathbf{y} = \{y_1, \dots, y_M\}^T, \boldsymbol{\tau} = \{\tau_1, \dots, \tau_N\}^T \text{ and } \boldsymbol{\pi} = \{\pi_1, \dots, \pi_M\}^T$$



Throughput Prediction Problem

The throughput prediction of \mathcal{Q} is the solution to this problem:

$$\arg \max_{\mathbf{y}} \left(\sum_{i=1}^N U_{f_i}(x_i) + \sum_{i=1}^M U_{q_i}(y_i) \right)$$

Subject to:

$$\begin{pmatrix} A & B \\ I & O \\ O & I \end{pmatrix} \begin{pmatrix} \mathbf{x} \\ \mathbf{y} \end{pmatrix} \leq \begin{pmatrix} \mathbf{c} \\ \boldsymbol{\tau} \\ \boldsymbol{\pi} \end{pmatrix}$$

Parameter Estimation

We consider the simpler form (let $\mathcal{Q} = \emptyset$ and ignore source constraints $\boldsymbol{\tau}$), replace $U_{f_i}(x)$ with Srikant's utility function:

$$\arg \max_{\boldsymbol{x}} \sum_{i=1}^N \left(\rho_i \frac{x_i^{1-\alpha_i}}{1-\alpha_i} \right)$$

Subject to:

$$A\boldsymbol{x} \leq \boldsymbol{c}$$

The solution $\hat{\boldsymbol{x}}$ can be considered as a function $\hat{\boldsymbol{x}}(\mathcal{F}, \boldsymbol{\alpha}; \boldsymbol{\rho})$ because the utility functions are **concave** and the domain is **convex**, or simply $\hat{\boldsymbol{x}}(\boldsymbol{\rho})$ for given \mathcal{F} and $\boldsymbol{\alpha}$.

Parameter Estimation (Cont.)

For a given set of flows \mathcal{F} , assume the α parameter in Srikant's utility function of each flow is known (denoted as α). Assume we have K samples $\tilde{\mathbf{x}}^{(1)}, \dots, \tilde{\mathbf{x}}^{(K)}$, the estimated ρ parameter of all flows (denoted as $\hat{\rho}$) is the solution of the following problem:

$$\hat{\rho} = \arg \min_{\rho} \frac{1}{2K} \sum_{k=1}^K \|\hat{\mathbf{x}}(\rho) - \tilde{\mathbf{x}}^{(k)}\|^2 \quad (\text{Minimize the error})$$

Practical Issues

- I1 To estimate throughput for all flows, we need a ρ_i for each possible (src, dst) pair. The number of **potential parameters** is large (H^2 for a network with H hosts)
- I2 Solving the parameter estimation problem by **compute gradient by definition** can be slow.
- I3 The estimation problem has not considered **source constraints** yet.
- I4 It is impractical to **monitor all the flows**. How to sample the traffic and extract useful information.

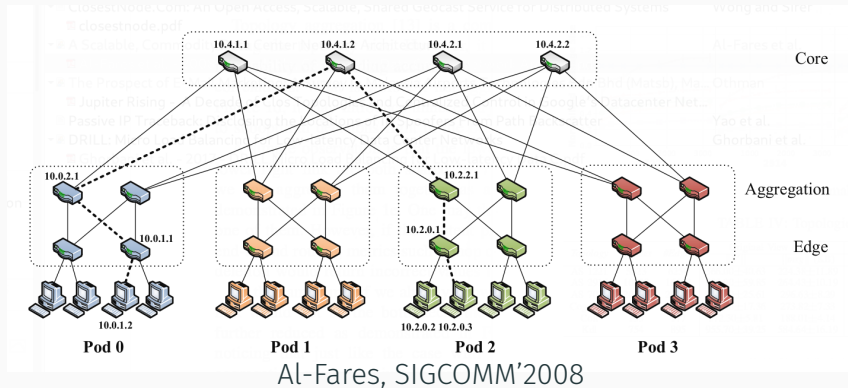
Optimizations

Practical Issues and How to Solve Them

- I1 To estimate throughput for all flows, we need a ρ_i for each possible (src, dst) pair. The number of potential parameters is large (H^2 for a network with H hosts)
Reduce #variables by dividing (src, dst) pairs into equivalent classes.
- I2 Solving the parameter estimation problem by compute gradient by definition can be slow.
- I3 The estimation problem has not considered source constraints (which might be unknown) yet.
- I4 It is impractical to monitor all the flows. How to sample the traffic and extract useful information.

Reduce the Number of Variables

- The utility function depends **only on the end-to-end cost**.
- In DCN, the topology is highly structured and many (src, dst) pairs have **similar end-to-end costs**.



Reduce the Number of Variables

Basic idea: Divide (src, dst) pairs to different equivalent classes

In a 3-layered fat tree topology, each host has 3 equivalent classes:

- In the same rack
- In the same Pod
- In different Pods

$3H$ parameters instead of H^2

Problem Transformation

Let ϱ_i^j represent the ρ parameter for the i -th equivalent class of j -th host, let $\bar{\rho} = \{\varrho_1^1, \varrho_2^1, \dots, \varrho_3^H\}$. Let p_i be the equivalent class index of f_i , we have $\rho_i = \bar{\rho}_{p_i}$ and its matrix form

$$\rho = \Lambda \bar{\rho} \quad \text{where} \quad \Lambda = \begin{bmatrix} \underbrace{0 \dots 0}_{p_1-1} & 1 & 0 & \dots & \dots & \dots \\ \vdots & & & \ddots & \ddots & \ddots \\ \underbrace{0 \dots \dots \dots 0}_{p_i-1} & 1 & 0 & \ddots & & \\ \vdots & & & \ddots & \ddots & \ddots \\ \underbrace{0 \dots \dots \dots 0}_{p_N-1} & 1 & 0 & \dots & \dots & \ddots \end{bmatrix}_{N \times 3H}$$

Parameter Estimation for Equivalent Classes

For a given set of flows \mathcal{F} , assume the α parameter in Srikant's utility function of each flow is known (denoted as α). Assume we have K samples $\tilde{\mathbf{x}}^{(1)}, \dots, \tilde{\mathbf{x}}^{(K)}$, the estimated $\bar{\rho}$ parameter of all equivalent classes (denoted as $\hat{\bar{\rho}}$) is the solution of the following problem:

$$\hat{\bar{\rho}} = \arg \min_{\bar{\rho}} \frac{1}{2K} \sum_{k=1}^K \|\hat{\mathbf{x}}(\Lambda \bar{\rho}) - \tilde{\mathbf{x}}^{(k)}\|^2 \quad (\text{Minimize the error})$$

Practical Issues and How to Solve Them

- I1 To estimate throughput for all flows, we need a ρ_i for each possible (src, dst) pair. The number of potential parameters is large (H^2 for a network with H hosts)
- I2 Solving the parameter estimation problem by compute gradient by definition can be slow.
Derive the gradient from KKT conditions.
- I3 The estimation problem has not considered source constraints (which might be unknown) yet.
- I4 It is impractical to monitor all the flows. How to sample the traffic and extract useful information.

Deriving the Gradient

We first consider the simplified NUM problem and according to **Karush-Kuhn-Tucker condition** (justified because the constraints are linear, i.e., the problem is LCQ):

$$\nabla_x f + \hat{\lambda}^T \nabla_x g = 0 \quad \Rightarrow \quad \forall j, \quad \bar{\rho}_{p_j} \hat{x}_j^{-\alpha_j} = \sum_k a_{kj} \hat{\lambda}_k, \quad (\text{Stationarity})$$

$$\hat{\lambda}^T g(\hat{x}) = 0 \quad \Rightarrow \quad \forall k, \quad \hat{\lambda}_k \left(\sum_j a_{kj} \hat{x}_j - c_k \right) = 0.$$

(Complementary Slackness)

Deriving the Gradient (cont.)

We now consider the **partial derivatives** of (Stationarity) and (Complementary Slackness) and after some reorganization, we have

$$\begin{pmatrix} \text{diag}(\bar{\rho}_{p_j} \alpha_j x_j^{-1-\alpha_j}) & A^T \\ \text{diag}(\lambda_k) A & \text{diag}(\sum_j a_{kj} x_j - c_k) \end{pmatrix} \begin{pmatrix} \mathbf{J}_x(\bar{\rho}) \\ \mathbf{J}_\lambda(\bar{\rho}) \end{pmatrix} = \begin{pmatrix} \Gamma \\ O \end{pmatrix}$$

where

$$\Gamma_{j,i} = \begin{cases} x_j^{-\alpha_j} & \text{if } p_j = i, \\ 0 & \text{if } p_j \neq i. \end{cases}$$

To be able to compute the gradient $\mathbf{J}_x(\bar{\rho})$, the leftmost matrix must be invertible.

Deriving the Gradient (cont.)

We let

$$\begin{pmatrix} M_1 & M_2 \\ M_3 & M_4 \end{pmatrix} = \begin{pmatrix} \text{diag}(\bar{\rho}_{p_j} \alpha_j x_j^{-1-\alpha_j}) & A^T \\ \text{diag}(\lambda_k) A & \text{diag}(\sum_j a_{kj} x_j - c_k) \end{pmatrix}.$$

M_1 is invertible, so we need to prove $\det(M_4 - M_3 M_1^{-1} M_2) \neq 0$.

$$(M_4 - M_3 M_1^{-1} M_2)_{ik} = \begin{cases} \sum_j a_{kj} \hat{x}_j - c_k - \hat{\lambda}_k \Phi_{kk}(\bar{\rho}) & \text{if } i = k \\ -\hat{\lambda}_i \Phi_{ik}(\bar{\rho}) & \text{otherwise} \end{cases}$$

where

$$\Phi_{ik}(\bar{\rho}) = \Phi_{ki}(\bar{\rho}) = \sum_j a_{ij} a_{kj} \bar{\rho}_{p_j}^{-1} \alpha_j^{-1} \hat{x}_j^{1+\alpha_j}.$$

Deriving the Gradient (cont.)

We can reorganize the matrix (by changing the order of constraints) by whether $\hat{\lambda}_k = 0$:

$$\det \begin{pmatrix} \text{diag}(\sum_j a_{kj} \hat{x}_j - c_k) & O \\ M'_1 & \text{diag}(\hat{\lambda}_k) M'_2 \end{pmatrix} = \prod_{\hat{\lambda}_k=0} \left(\sum_j a_{kj} \hat{x}_j - c_k \right) \prod_{\hat{\lambda}_k \neq 0} \hat{\lambda}_k \det(M'_2)$$

- If $\hat{\lambda}_k = 0$, usually $\sum_j a_{kj} \hat{x}_j - c_k \neq 0$. Otherwise, we can add a disruption to c_k to make sure $\sum_j a_{kj} \hat{x}_j - c_k \neq 0$ **without affecting the solutions**.
- $\det(M'_2)$ is a polynomial of $\bar{\rho}$, it will not always be zero.

With a small disruption, we ensure the matrix is full-rank. So we use numerical methods to get $\mathbf{J}_{\hat{x}}(\bar{\rho})$.

Deriving the Gradient (cont.)

With $\mathbf{J}_{\hat{\mathbf{x}}}(\bar{\boldsymbol{\rho}})$, we can derive the gradient of the error function as:

$$\nabla E = \frac{1}{K} \sum_{k=1}^K (\hat{\mathbf{x}} - \tilde{\mathbf{x}}^{(k)})^T \mathbf{J}_{\hat{\mathbf{x}}}(\bar{\boldsymbol{\rho}})$$

In practice, we use spherical coordinates to avoid choosing step sizes. The final gradient is

$$\nabla_{\phi} E = \frac{1}{K} \sum_{k=1}^K (\hat{\mathbf{x}} - \tilde{\mathbf{x}}^{(k)})^T \mathbf{J}_{\hat{\mathbf{x}}}(\bar{\boldsymbol{\rho}}) \mathbf{J}_{\bar{\boldsymbol{\rho}}}(\boldsymbol{\phi})^T$$

Practical Issues and How to Solve Them

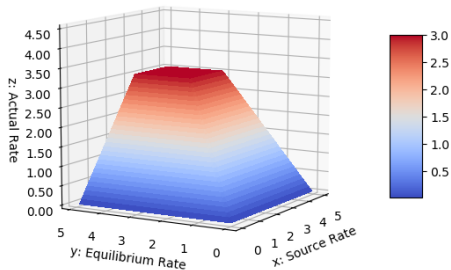
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- I2 Solving the parameter estimation problem by compute gradient by definition can be slow.
- I3 The estimation problem has not considered source constraints (which might be unknown) yet.
Consider effective source constraints through lazy identification.
- I4 It is impractical to monitor all the flows. How to sample the traffic and extract useful information.

Handling Unknown Source Constraints

Basic idea: Consider only the *effective* source constraints.

A sample might be constrained by an **effective** source constraint if:

- Sampled throughput is significantly smaller than the estimated throughput (of the same equivalent class).
- Sampled throughput is at a relatively fixed rate.



Practical Issues and How to Solve Them

- I1 To estimate throughput for all flows, we need a ρ_i for each possible (src, dst) pair. The number of potential parameters is large (H^2 for a network with H hosts)
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Consider low-throughput flows as non-reactive flows.

Sampling

Basic idea: Identify individual *throughput-sensitive* flows and accumulate the *low-throughput* flows.

Short-lived and low-throughput flows may not reach the equilibrium and their throughput cannot be measured very accurately. But many short-lived, low-throughput flows cannot be ignored.

Solution

Extract the individual flows with more than 5% of the total link capacity as samples and compute the accumulated traffic demand from the rest. Let v_k be the traffic demand on the k -th link, the link capacity used in the prediction is computed as $c_k - v_k$.

Evaluation

Settings

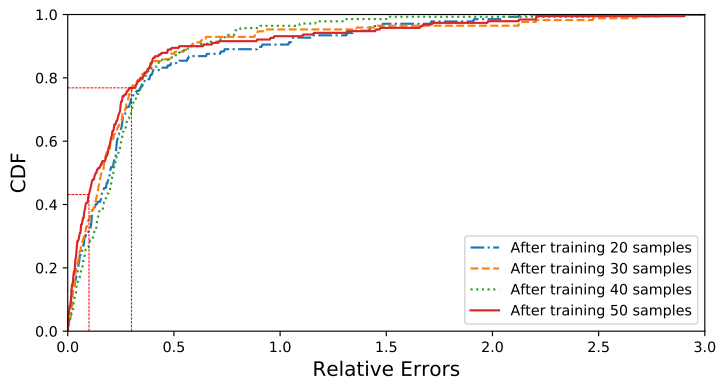
Topology: A Clos topology with $K = 4$, 16 hosts (32 links)

Flows: 100 initial flows, 60 samples each with 10-20 flows.

- We use **NS2** to run the traffic and get the throughput for each sample. The parameter estimation and prediction are analyzed **offline**.
- Each sample is first used as a query to measure the **prediction error** and **prediction time**.
- We update the ρ every sample and measure the **estimation time**.

Prediction Accuracy (Vegas)

Metric: Relative errors: $\left| \frac{\tilde{x} - \hat{x}}{\tilde{x}} \right|$

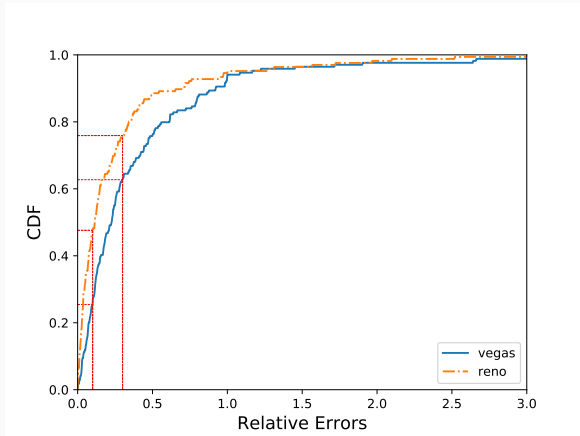


>75% flows have a smaller relative error than 30%.

Prediction Accuracy (Multiple TCP)

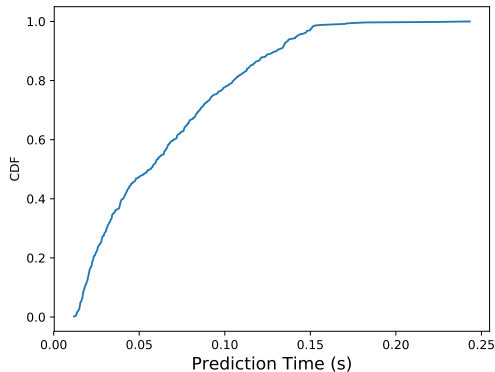
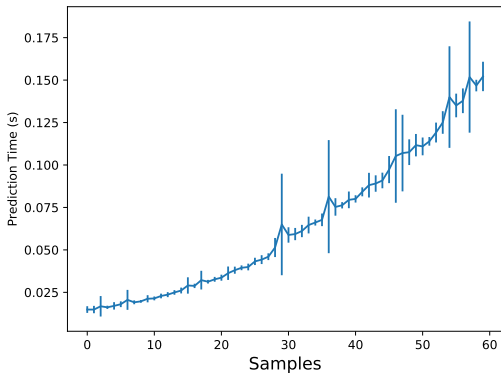
Metric: Relative errors: $\left| \frac{\tilde{x} - \hat{x}}{\tilde{x}} \right|$

- Predictions become less accurate (60%/75% with relative error smaller than 30%)
- Prediction for TCP Reno is more accurate than Vegas



Prediction Time

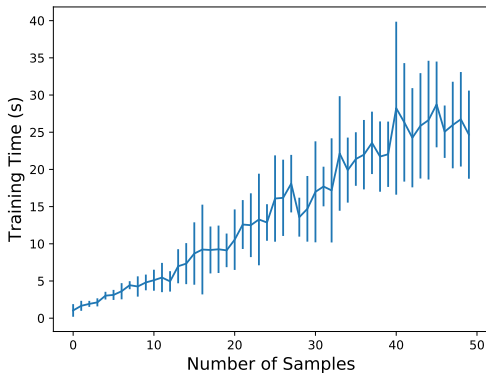
Metric: The time used to conduct a prediction



Less than 0.2s for up to 1056 flows (19 fg and 1037 bg).

Parameter Estimation Convergence

Metric: The time used to get an optimal parameter estimation.



Discussions

A Model-Driven Throughput Prediction System

- Predict throughput by solving NUM problem
- Handle heterogeneity with unified utility functions (Srikant's utility function)
- Obtain traffic samples with advanced monitoring techniques (Per-flow monitoring)
- Estimate unknown parameters ρ using the gradient descent method

Limitations

Overall Framework

- Limited to special network topologies and special TCP variants.

Optimization

- Impact of multiple paths between two hosts is not analyzed.
- Convergence of the parameter estimation is not proved.
- Mistakes in the published paper (corrected in this presentation).

Evaluation

- Not enough real traffic analysis

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Revisit the Assumptions

- DC Network

What about an arbitrary network?

- Vegas and Reno

What about other TCP congestion control algorithms?

- Random Sampling

Are there better sampling methods?

Revisit the Assumptions

- DC Network

What about an arbitrary network?

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What about other TCP congestion control algorithms?

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Are there better sampling methods?

Possible directions:

- In SDN, get routing matrix and propagation delay from the controller.
- Use function approximation to model the utility function for arbitrary TCP variants.
- Sketch-based sampling

Parameter Estimation: How to Get Unique ρ

A minimal example:

$$A = \begin{pmatrix} 100 \\ 110 \\ 101 \end{pmatrix}, \mathbf{c} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \boldsymbol{\alpha} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \tilde{\mathbf{x}} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$$

There are actually **multiple** ρ s which minimizes the estimation error as long as:

$$\begin{aligned} \rho_1 &= \frac{1}{3} (2 + x_1 - x_2 - x_3) \\ \rho_2 + \rho_3 &= \frac{1}{3} (1 - x_1 + x_2 + x_3) \end{aligned}$$

A Model-Driven Throughput Prediction System

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Q & A

We'd like to thank the reviewers for their insightful feedback!

Questions and comments are highly appreciated!

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Prophet

A Model-Driven Throughput Prediction System

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