



**NOVA:**

# Towards On-Demand Equivalent Network View Abstraction for Network Optimization

---

*Kai Gao*<sup>23</sup>, *Qiao Xiang*<sup>13</sup>, *Xin Wang*<sup>13</sup>, *Yang Richard Yang*<sup>13</sup> and *Jun Bi*<sup>2</sup>

<sup>1</sup>Department of Computer Science, Tongji University

<sup>2</sup>Institute for Network Science and Cyberspace, Tsinghua University

<sup>3</sup>Department of Computer Science, Yale University

# Table of Contents

1. Introduction

2. NOVA

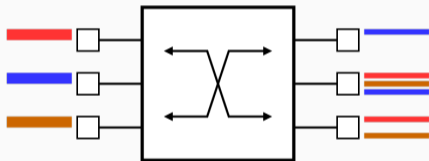
3. Summary

# Introduction

---

# A Motivating Example

- Three requests: red (r), blue (b) and brown (y)

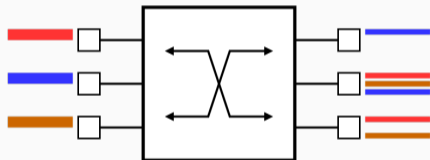


## A Motivating Example

- Three requests: red (r), blue (b) and brown (y)
- Private QoS function:

$$\frac{1}{\alpha \times \text{hopcount} + \frac{\beta}{\text{bandwidth}}}$$

- Local preference: red request is from a privileged client



# Existing Work

- Centralized optimization framework for SDN
  - Example: SOL<sup>1</sup>
  - Limitation: Require applications to submit private information

---

<sup>1</sup>Victor Heorhiadi, Michael K Reiter, and Vyas Sekar. “Simplifying Software-Defined Network Optimization Using SOL”, NSDI’16

# Existing Work

- Centralized optimization framework for SDN
- Global view
  - Example: NOX<sup>1</sup>
  - Limitation: Contain redundant information even after filtering, leak sensitive network information (topology),

---

<sup>1</sup>Natasha Gude et al. "NOX: towards an operating system for networks", SIGCOMM CCR'08

# Existing Work

- Centralized optimization framework for SDN
- Global view
- One-Big Switch<sup>1</sup>
  - Example: CoFlow<sup>2</sup>, VL2<sup>3</sup>
  - Limitation: Assume no bottleneck inside the network, cannot present end-to-end information

---

<sup>1</sup>Nanxi Kang et al. "Optimizing the "one big switch" abstraction in software-defined networks", CoNEXT'13

<sup>2</sup>Mosharaf Chowdhury and Ion Stoica. "Coflow: A networking abstraction for cluster applications", HotNet'12

<sup>3</sup>Albert Greenberg et al. "VL2: a scalable and flexible data center network", SIGCOMM'09



## Existing Work

- Centralized optimization framework for SDN
- Global view
- One-Big Switch
- End-to-end map abstraction
  - Example: ALTO<sup>1</sup>
  - Limitation: Cannot present shared bottleneck

---

<sup>1</sup>Richard Alimi, Yang Yang, and Reinaldo Penno. "Application-layer traffic optimization (ALTO) protocol", RFC 7285

## Requirements:

- *Constructed on demand*
- *Without loss of information*
- *Protecting sensitive information*
- *Compact in size*

## Requirements:

- Constructed on demand
- Without loss of information
- Protecting sensitive information
- Compact in size

## The NOVA abstraction is

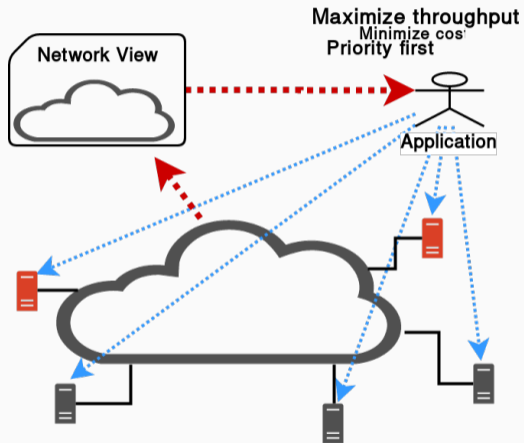
- Based on **flow queries**
- Using **equivalent** transformation
- Using **irreversible** transformation
- Reducing **redundant** information as much as possible

**NOVA**

---

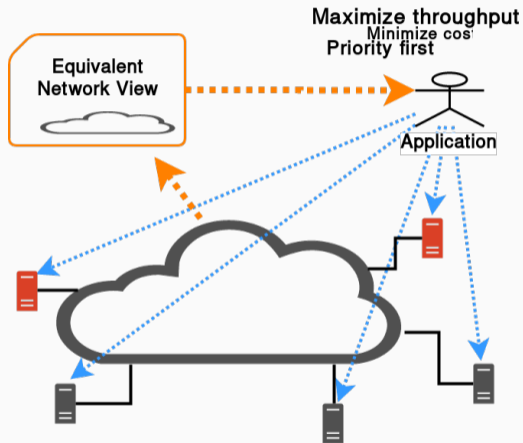
# Key Observation

- Observation: Applications use network views to make **traffic scheduling** decisions to achieve a certain **objective**.

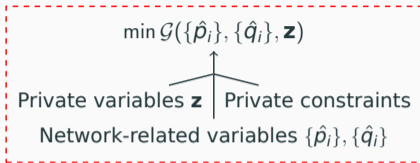


# Key Observation

- Observation: Applications use network views to make **traffic scheduling** decisions to achieve a certain **objective**.
- Conclusion: Equivalent network views allow applications to always make the *same* optimal decision.



# Application-Network Collaborative Optimization Model



$F$ : set of flows

**Application**

---

**Network**

Routing policies, topology, etc.

Application objective function  
template:

$$\min \mathcal{E}(\{\hat{\rho}_i\}, \{\hat{q}_i\})$$

# Application-Network Collaborative Optimization Model

$$\min \mathcal{E}(\{\hat{p}_i\}, \{\hat{q}_i\})$$

$F$ : set of flows

**Application**

-----  
**Network**

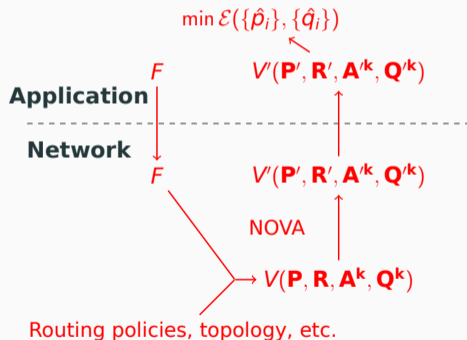
Routing policies, topology, etc.

Application objective function  
template:

$$\min \mathcal{E}(\{\hat{p}_i\}, \{\hat{q}_i\})$$



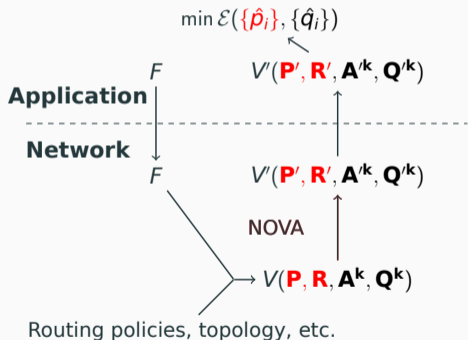
# Application-Network Collaborative Optimization Model



Network processing:

- Take flow request  $F$  and return a subset of global view  $V$
- NOVA kicks in and produces the equivalent view  $V'$

# Application-Network Collaborative Optimization Model



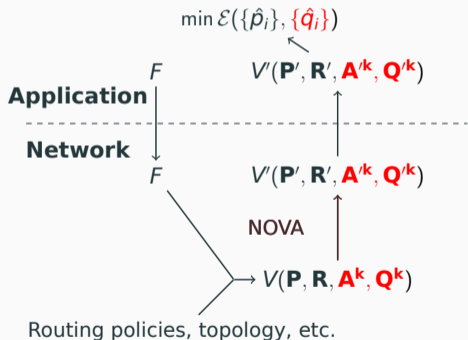
End-to-End metrics ( $\hat{p}_i$ ):

- Accumulated along the forwarding paths
- Values are (statistically) independent of flows
- Based on **Variant QoS metric algebra**: extended from *Sobrinho's QoS algebra*<sup>2</sup>, **relaxed path concatenation** to **linearize QoS metrics**

$$\hat{\mathbf{P}} = \mathbf{R} \times \mathbf{P}$$

<sup>2</sup>João Luís Sobrinho. "Algebra and algorithms for QoS path computation and hop-by-hop routing in the Internet", TON'02

# Application-Network Collaborative Optimization Model



Shared resources ( $\hat{q}_i$ ):

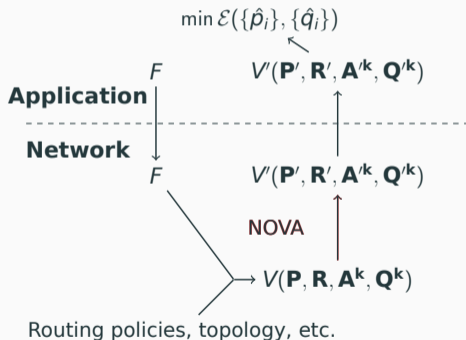
- Constrained by resources available on the forwarding paths
- Shared by different flows

$$\mathbf{A}^k \times \hat{\mathbf{q}}^k \leq \mathbf{q}^k$$

# Application-Network Collaborative Optimization Model

Common constraints:

$$\mathbf{R} \geq 0, \mathbf{A}^k \geq 0, \mathbf{q}^k \geq 0, \mathbf{q}^k \geq 0$$



## Equivalent Network View

A declarative definition (**what we want to achieve**):

- Applications can use the view to make the same traffic scheduling decision.

# Equivalent Network View

A declarative definition (**what we want to achieve**):

- Applications can use the view to make the same traffic scheduling decision.

A mathematical definition (**how we verify the equivalence**):

- End-to-End metrics:

$$\mathbf{R}_1 \times \mathbf{P}_1 = \mathbf{R}_2 \times \mathbf{P}_2$$

- Shared resources:

$$F_1^k = \left\{ \mathbf{x} \mid \mathbf{A}_1^k \mathbf{x} \leq \mathbf{q}_1^k \right\} = \left\{ \mathbf{x} \mid \mathbf{A}_2^k \mathbf{x} \leq \mathbf{q}_2^k \right\} = F_2^k$$

# Basic Equivalent Transformations

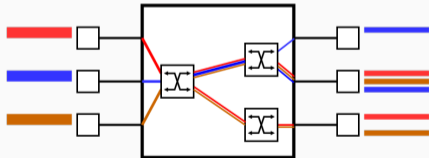
NOVA

$$V(\mathbf{P}, \mathbf{R}, \mathbf{A}^k, \mathbf{Q}^k) \longrightarrow V'(\mathbf{P}', \mathbf{R}', \mathbf{A}'^k, \mathbf{Q}'^k)$$

A series of **basic transformations**

Network view used in the example:

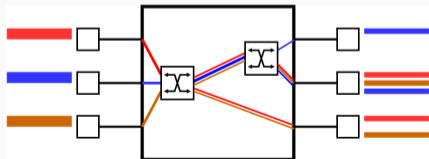
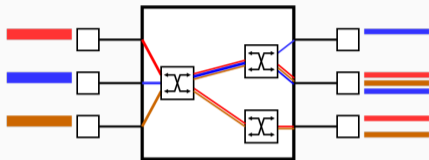
$\mathbf{R}(\mathbf{A}^T)$	$e_1$	$e_2$	$e_3$	$e_4$	$e_5$	$e_6$	$e_7$	$e_8$
$r_1$	1	0	0	1	0	0	1	0
$r_2$	1	0	0	0	1	0	0	1
$b_1$	0	1	0	1	0	1	0	0
$b_2$	0	1	0	1	0	0	1	0
$y_1$	0	0	1	1	0	0	1	0
$y_2$	0	0	1	0	1	0	0	1
hop	1	1	1	1	1	1	1	1
bw	100	100	100	150	150	70	70	70



# Basic Transformation Example: Aggregation

- Equivalence condition: Same row vector  $\mathbf{R}_j^T$  &  $\mathbf{A}_j^k$
- Merge columns with **variant QoS metric algebra**

$\mathbf{R}(\mathbf{A}^T)$	$e_1$	$e_2$	$e_3$	$e_4$	$e_5$	$e_6$	$e_7$	$e_8$
$r_1$	1	0	0	1	0	0	1	0
$r_2$	1	0	0	0	1	0	0	1
$b_1$	0	1	0	1	0	1	0	0
$b_2$	0	1	0	1	0	0	1	0
$y_1$	0	0	1	1	0	0	1	0
$y_2$	0	0	1	0	1	0	0	1
hop	1	1	1	1	1	1	1	1
bw	100	100	100	150	150	70	70	70

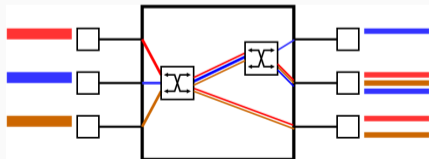
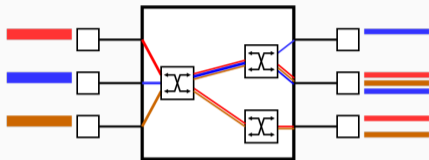




# Basic Transformation Example: Aggregation

- Equivalence condition: Same row vector  $\mathbf{R}_j^T$  &  $\mathbf{A}_j^k$
- Merge columns with **variant QoS metric algebra**

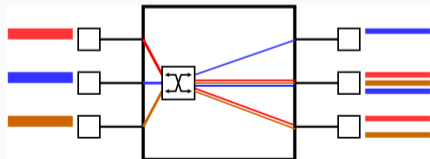
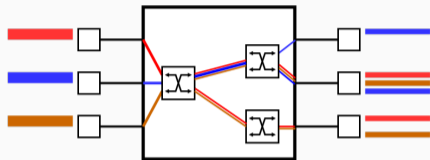
$\mathbf{R}(\mathbf{A}^T)$	$e_1$	$e_2$	$e_3$	$e_4$	$e_6$	$e_7$	$e_8$
$r_1$	1	0	0	1	0	1	0
$r_2$	1	0	0	0	0	0	1
$b_1$	0	1	0	1	1	0	0
$b_2$	0	1	0	1	0	1	0
$y_1$	0	0	1	1	0	1	0
$y_2$	0	0	1	0	0	0	1
hop	1	1	1	1	1	1	2
bw	100	100	100	150	70	70	70



# Basic Transformation Example: Decomposition

- Equivalence condition:  $\mathbf{A}_j^k \mathbf{x} \leq q_j^k$  is **redundant** and  $\mathbf{R}_j = \sum_r \mathbf{R}_j^{(r)}$ ,  $\mathbf{A}_j^k = \sum_r \mathbf{A}_j^{k(r)}$
- Split columns so that new columns can be aggregated

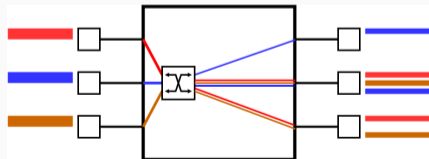
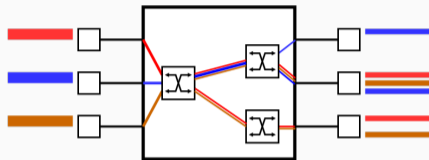
$\mathbf{R}(\mathbf{A}^T)$	$e_1$	$e_2$	$e_3$	$e_4$	$e_6$	$e_7$	$e_8$
$r_1$	1	0	0	1	0	1	0
$r_2$	1	0	0	0	0	0	1
$b_1$	0	1	0	1	1	0	0
$b_2$	0	1	0	1	0	1	0
$y_1$	0	0	1	1	0	1	0
$y_2$	0	0	1	0	0	0	1
hop	1	1	1	1	1	1	2
bw	100	100	100	150	70	70	70



# Basic Transformation Example: Decomposition

- Equivalence condition:  $\mathbf{A}_j^k \mathbf{x} \leq q_j^k$  is **redundant** and  $\mathbf{R}_j = \sum_r \mathbf{R}_j^{(r)}$ ,  $\mathbf{A}_j^k = \sum_r \mathbf{A}_j^{k(r)}$
- Split columns so that new columns can be aggregated

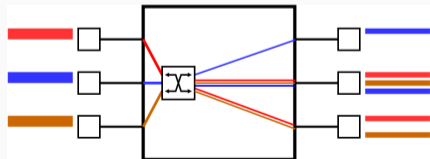
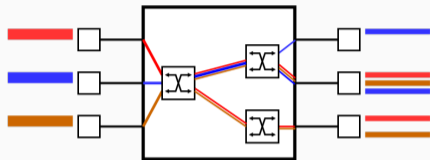
$\mathbf{R}(\mathbf{A}^T)$	$e_1$	$e_2$	$e_3$	$e_4^1$	$e_4^2$	$e_6$	$e_7$	$e_8$
$r_1$	1	0	0	0	1	0	1	0
$r_2$	1	0	0	0	0	0	0	1
$b_1$	0	1	0	1	0	1	0	0
$b_2$	0	1	0	0	1	0	1	0
$y_1$	0	0	1	0	1	0	1	0
$y_2$	0	0	1	0	0	0	0	1
hop	1	1	1	1	1	1	1	2
bw	100	100	100	150	150	70	70	70



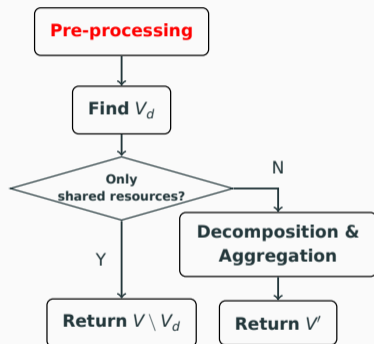
# Basic Transformation Example: Decomposition

- Equivalence condition:  $\mathbf{A}_j^k \mathbf{x} \leq q_j^k$  is **redundant** and  $\mathbf{R}_j = \sum_r \mathbf{R}_j^{(r)}$ ,  $\mathbf{A}_j^k = \sum_r \mathbf{A}_j^{k(r)}$
- Split columns so that new columns can be aggregated

$\mathbf{R}(\mathbf{A}^T)$	$e_1$	$e_2$	$e_3$	$e_6$	$e_7$	$e_8$
$r_1$	1	0	0	0	1	0
$r_2$	1	0	0	0	0	1
$b_1$	0	1	0	1	0	0
$b_2$	0	1	0	0	1	0
$y_1$	0	0	1	0	1	0
$y_2$	0	0	1	0	0	1
hop	1	1	1	2	2	2
bw	100	100	100	70	70	70



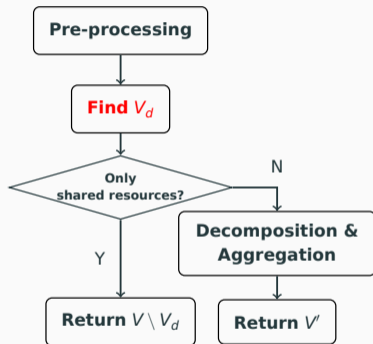
# Overall Algorithm



Aggregate columns with the same row vector  $(R_j^T, A_j^k)$

- A pre-processing step
- Avoid corner case in redundancy check (identical constraints)

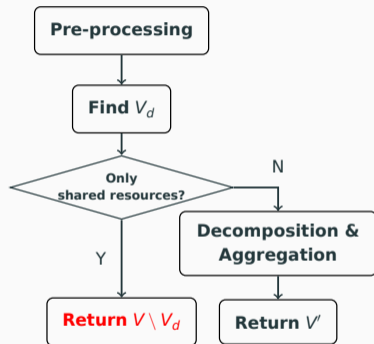
# Overall Algorithm



Find decomposable columns  $V_d$

- Equivalent to finding redundant linear constraints
- Well-studied problem

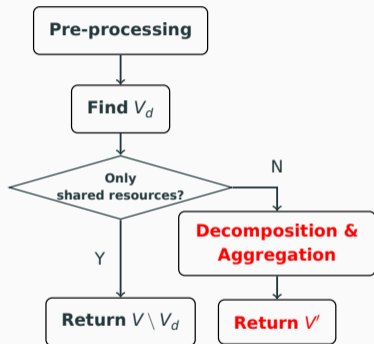
# Overall Algorithm



Check if only shared resources are requested

- Equivalent to One-big switch abstraction if no bottlenecks are within the network

# Overall Algorithm

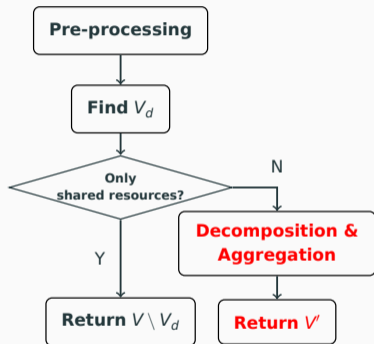


Decompose  $\forall v \in V_d$  with unit basis

- Bounded size ( $|V| - |V_d| + |F|$ )
- Low computation overhead  $O(|V_d||F|)$
- **Equivalent to end-to-end abstraction** if  $V = V_d$  (only end-to-end metrics are requested)



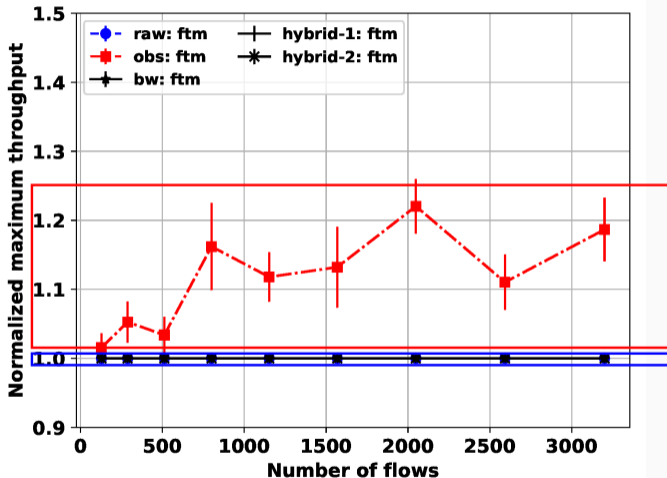
# Overall Algorithm



Techniques to improve performance:

- Reduce space overhead: Aggregate the new columns **immediately**
- Leverage parallel processing: Use Map-Reduce-like **divide-and-conquer**

# Evaluation: Verifying Equivalence

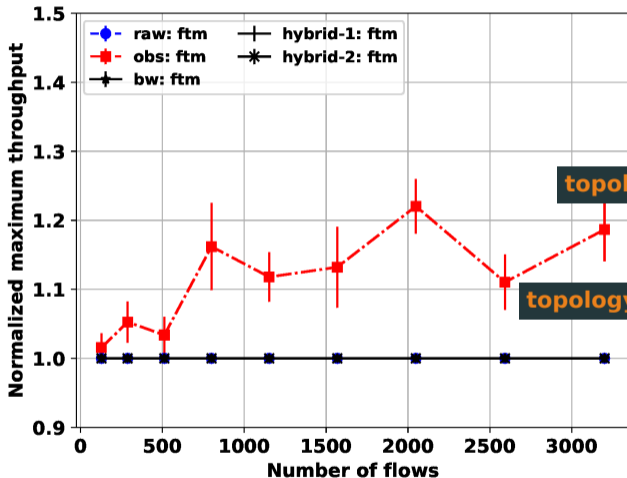


topology: Kdl traffic pattern: few-to-many

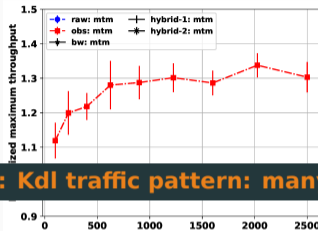
**One-big switch:  
infeasible solution**

**NOVA:  
overlap with raw network view**

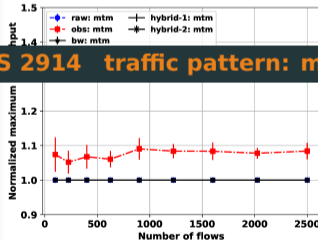
# Evaluation: Verifying Equivalence



**topology: Kdl traffic pattern: few-to-many**



**topology: Kdl traffic pattern: many-to-many**



**topology: AS 2914 traffic pattern: many-to-many**

## Evaluation: Effective Factors

- Topology
- Traffic pattern
- Number of flows
- Redundancy check algorithm

## Evaluation: Effective Factors

- Topology
- Traffic pattern
- Number of flows
- Redundancy check algorithm

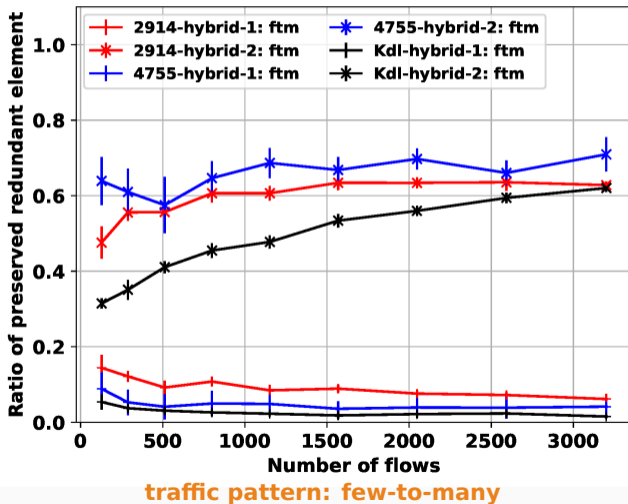
Determined by the nature of the network and the application

## Evaluation: Effective Factors

- Topology
- Traffic pattern
- Number of flows
- Redundancy check algorithm

Can be controlled by NOVA

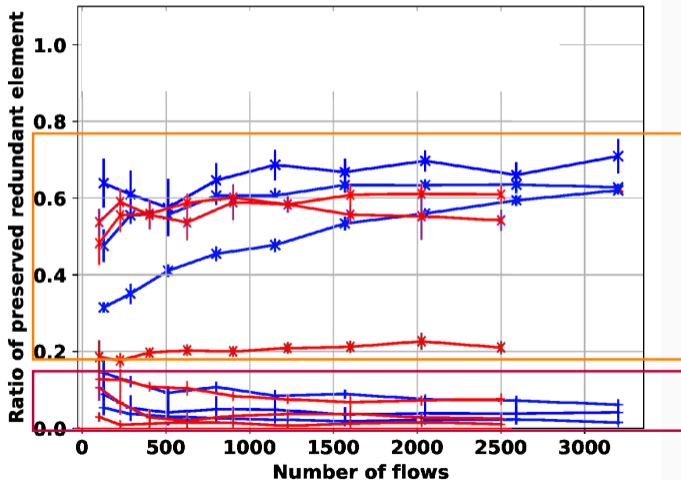
## Normalized redundancy preservation



Topology can effect the redundancy preservation

# Evaluation: Traffic Pattern

## Redundancy preservation



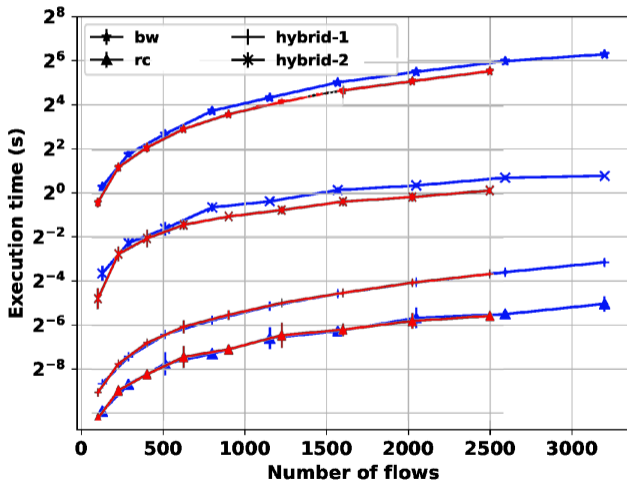
**Relaxed redundancy check:**  
**Many-to-many** has better  
reduction ratio than  
**few-to-many**

**Strict redundancy check:**  
**No significant difference**



# Evaluation: Traffic Pattern

## Computation overhead

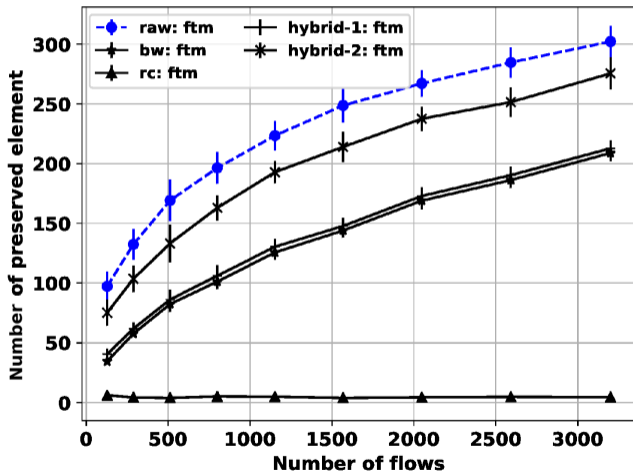


topology: AS 2914, 8 threads

**Few-to-many and many-to-many patterns have no significant difference**

# Evaluation: Number of flows

## Redundancy reduction

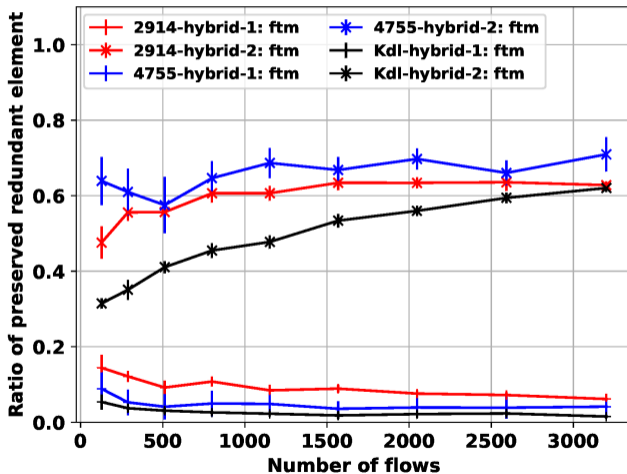


More flows,  
more preserved elements  
more information leaked

topology: AS 4755, traffic pattern: few-to-many

# Evaluation: Number of flows

## Redundancy reduction

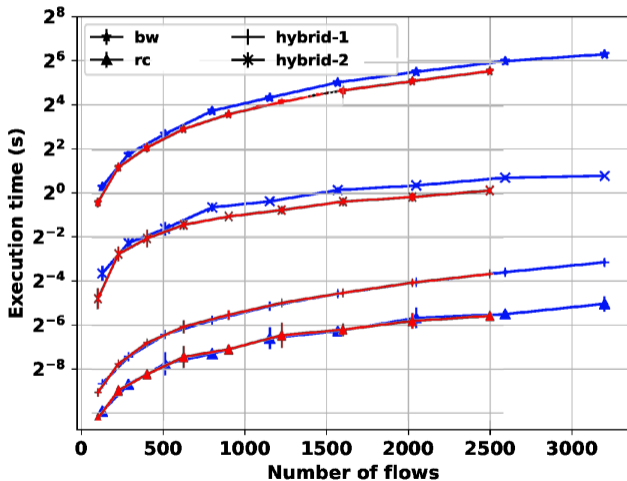


traffic pattern: few-to-many

Effect on reduction ratio depends on topology and redundancy check algorithm

# Evaluation: Number of flows

## Computation overhead

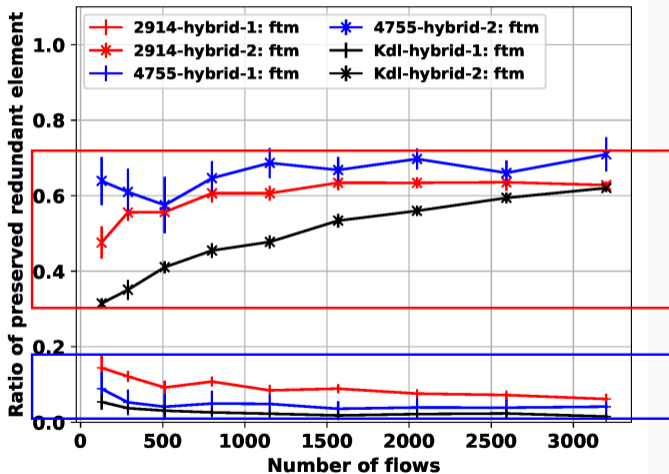


topology: AS 2914, 8 threads

More flows,  
larger computation time

# Evaluation: Redundancy Check Algorithm

## Normalized redundancy preservation



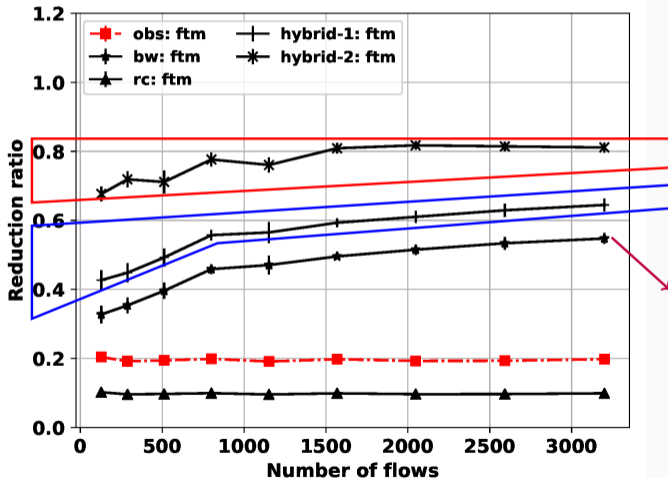
traffic pattern: few-to-many

Relaxed redundancy check:  
More remaining  
redundant elements

Strict redundancy check:  
Less remaining  
redundant elements

# Evaluation: Redundancy Check Algorithm

## Normalized communication overhead



**Relaxed redundancy check:**  
Larger overhead ( $\sim 4x$  OBS)

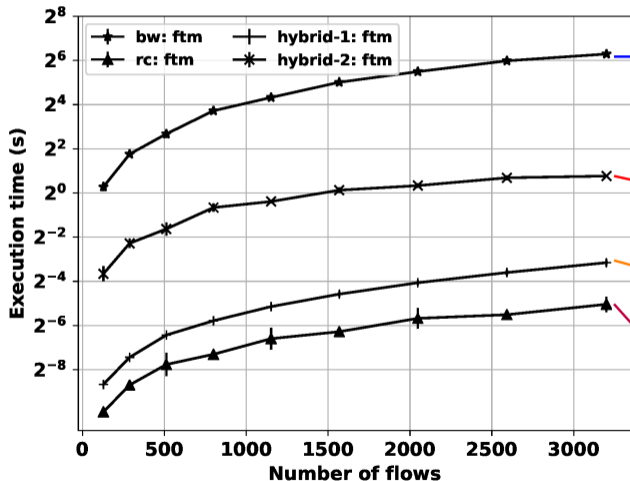
**Strict redundancy check:**  
Smaller overhead ( $\sim 3x$  OBS)

Optimal size without  
information loss

topology: AS 2914, traffic pattern: few-to-many

# Evaluation: Redundancy Check Algorithm

## Computation overhead



**Time of strict redundancy check algorithm**  
(~ 5s for ~500 flows)

**Time of relaxed redundancy check algorithm**  
(<3s for ~3000 flows)

**Time of decomposition & aggregation**

**Time to compute  $P \times R$**   
(Routing cost only)

topology: AS 2914, traffic pattern: few-to-many, 8 threads

## Evaluation: Effective Factors

- **Topology**
  - **Traffic pattern**
  - **Number of flows**
  - **Redundancy check algorithm**
- 
- Can effect the reduction ratio and computation time
  - Usually does not change



## Evaluation: Effective Factors

- **Topology**
  - **Traffic pattern**
  - **Number of flows**
  - **Redundancy check algorithm**
- 
- Mostly effect the relaxed redundancy check algorithm
  - No significant correlations on computation time
  - Usually does not change

## Evaluation: Effective Factors

- **Topology**
  - **Traffic pattern**
  - **Number of flows**
  - **Redundancy check algorithm**
- 
- More flows, more information leaked, more communication overhead and computation time
  - Mostly effect the relaxed redundancy check algorithm

## Evaluation: Effective Factors

- **Topology**
- **Traffic pattern**
- **Number of flows**
- **Redundancy check algorithm**
  
- **Strict redundancy check:** Better privacy protection, less communication overhead, more computation overhead
- **Relaxed redundancy check:** More information leaked, more communication overhead, less computation overhead

# Summary

---

## Summary and Future Work

In this paper, we

- Identify the problem of providing on-demand network views and the limitations of existing works
- Extend the QoS metric algebra and model the **Application-Network Collaborative Optimization**
- Define **equivalent network view** and design novel and efficient algorithms to construct it

# Conclusion

Evaluations show that:

- NOVA produces equivalent network view
- NOVA can effectively reduce redundant information and communication overhead with strict redundancy check algorithm
- NOVA can differentiate privacy by choosing different redundancy check algorithms and limiting the number of flows in a request

- From a single user to multiple users
- From predetermined paths to application-aware path optimization
- From fixed reserved resource to dynamic resource allocation
- From simulated results to real running use cases

**Thank you!**

**Q & A**



# QoS Metric Algebra

“Routing algebra” by Sobrinho<sup>2</sup>:  $(P, S, w, \circ, \oplus, \preceq)$

- $P$ : Set of paths
- $S$ : Range of a metric
- $w : P \mapsto S$ : Weight function
- $\circ : P \times P \mapsto P$ : Concatenation operator
- $\oplus : S \times S \mapsto S$ : Logical “plus” operator
- $\preceq : S \times S \mapsto \{0, 1\}$ : Logical “compare” operator

---

<sup>2</sup>João Luís Sobrinho. “Algebra and algorithms for QoS path computation and hop-by-hop routing in the Internet”. In: *IEEE/ACM Transactions on Networking (TON)* 10.4 (2002). 00328, pp. 541–550.

# QoS Metric Algebra

Variant metric algebra:  $(P, S, w, \circ, \oplus, \preceq, \otimes)$

- $P$ : Set of paths
- $S$ : Range of a metric
- $w : P \mapsto S$ : Weight function
- $\oplus : S \times S \mapsto S$ : Logical “plus” operator
- $\otimes : \mathbb{R} \times S \mapsto S$ : Logical “multiply” operator

# QoS Metric Algebra Examples

**Table 1:** The Variant Routing Metric Algebra.

S	Weight function ( $w$ )	$w(p_1)$	$w(p_2)$	$w(p_1 \circ p_2)$	$N \otimes w(p_1)$	Identity ( $e$ )	Zero ( $\mathbf{0}$ )
$\mathbb{N}^+$	Hopcount	$h_1$	$h_2$	$h_1 + h_2$	$N \cdot h_1$	0	$+\infty$
$\mathbb{R}^+$	Bandwidth	$b_1$	$b_2$	$\min(b_1, b_2)$	$b_1$	$+\infty$	0
$\mathbb{R}^+$	Delay	$d_1$	$d_2$	$d_1 + d_2$	$N \cdot d_1$	0	$+\infty$
[0, 1]	Loss rate	$r_1$	$r_2$	$1 - (1 - r_1)(1 - r_2)$	$1 - (1 - r_1)^N$	0	1